



# **TEKNIK MENJAWAB MATEMATIK TAMBAHAN 2015**

# Pengagihan Nisbah Soalan dalam Matematik Tambahan SPM

- R : S : T
- 6 : 3 : 1      Kertas 1
- 4 : 3 : 3      Kertas 2



# **Mengetahui Format Kertas Soalan**

## **Memahami Format Kertas Soalan SPM**

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**Kertas 1 ( 2 jam )**

**( 25 soalan) wajib**

**Aras Kesukaran R:S:T = 6:3:1**

**Kertas 2 ( 2 jam 30 min)**

**Bahagian A : 6 soalan wajib**

**Aras Kesukaran  
R:S:T = 4:3:3**

**Bahagian B : 5 soalan pilih 4**

**Bahagian C : 4 soalan pilih 2**



# **SOALAN KERTAS 1**

**Semua topik kecuali 4 topik di bahagian C Kertas 2 iaitu**

- Pengaturcaraan Linear
- Gerakan Pada Garis Lurus
- Penyelesaian Segitiga
- Nombor Indeks



# KERTAS 2

- **BAHAGIAN A (6 SOALAN, 40%)**

- Persamaan Serentak
- Persamaan Kuadratik / Fungsi Kuadratik
- Pembezaan / Pengamiran
- Statistik / Vektor
- Sukatan Membulat
- Indeks dan Logaritma
- Fungsi Trigonometri
- Janjang



# KERTAS 2

## **BAHAGIAN B : ( 5 PILIH 4, 40%)**

- Hukum Linear
- Pengamiran (Luas & Isipadu)
- Taburan Binomial & Taburan Normal
- Geometri Koordinat
- Fungsi Trigonometri
- Vektor
- Janjang
- Indeks dan Logaritma



## KERTAS 2

BAHAGIAN C : ( 4 PILIH 2, 20%)

- Pengaturcaraan Linear
- Gerakan Pada Garis Lurus
- Penyelesaian Segitiga
- Nombor Indeks



# 9 TOPIK YANG SENANG

- Fungsi
- Persamaan Kuadratik
- Fungsi Kuadratik
- Persamaan Serentak
- Indeks dan Logaritma
- Statistik
- Hukum Linear
- Geometri Koordinat
- Nombor Indeks



<b>Topik</b>	<b>Kertas 1</b>	<b>Kertas 2</b>
Fungsi	9	
Persamaan Kuadratik	3	
Fungsi Kuadratik	6	
Persamaan Serentak		5
Indeks dan Logaritma	7	4
Statistik		8
Hukum Linear	4	10
Geometri Koordinat	3	7
Nombor Indeks		10
Jumlah Markah	32/80	44/100

Jumlah Markah Keseluruhan pada tahun 2011 : **42.2 %**

<b>Topik</b>	<b>Kertas 1</b>	<b>Kertas 2</b>
Fungsi	9	
Persamaan Kuadratik	6	
Fungsi Kuadratik	3	
Persamaan Serentak		5
Indeks dan Logaritma	6	
Statistik	3	6
Hukum Linear	4	10
Geometri Koordinat	6	10
Nombor Indeks		10
Jumlah Markah	37/80	41/100

Jumlah Markah Keseluruhan pada tahun 2012 : **42.8 %**

Topik	Kertas 1	Kertas 2
Fungsi	9	
Persamaan Kuadratik	6	
Fungsi Kuadratik	3	
Persamaan Serentak		5
Indeks dan Logaritma	6	
Statistik	3	7
Hukum Linear	4	10
Geometri Koordinat	6	10
Nombor Indeks		10
Jumlah Markah	37/80	42/100

Jumlah Markah Keseluruhan pada tahun 2013 : 43.9 %

# **Contoh Soalan Kertas 1**



1.  $f(x) = x^2 + 4x + 7$
- (A) CARI NILAI MAKSIMUM ATAU NILAI MINIMUM BAGI FUNGSI
- (B) NYATAKAN PERSMAAN PAKSI SIMETRI BAGI GRAF F(X).
- [4 marks]

***Penyelesaian***

- $f'(x) = 2x + 4 = 0$  B1
- $x = -2$
- $f(-2) = (-2)2 + 4(-2) + 7 = 3$  B1
  
- 
- (a) Min. Value =3 B1
- (b)  $x = -2$  B1

SELESAIKAN.

$$8^x = 16^{x-3}$$

[3 marks]

Penyelesaian

$$\textcircled{O} \quad 8^x = 16^{x-3}$$

$$\textcircled{O} \quad (2^3)^x = 2^{4(x-3)} \quad \text{B1}$$

$$\textcircled{O} \quad 2^{3x} = 2^{4x-12}$$

$$\textcircled{O} \quad 3x = 4x - 12 \quad \text{B1}$$

$$\textcircled{O} \quad x = 12 \quad \text{B1}$$



$$\log_5(4x - 7) = \log_5(x - 2) + 1.$$

[3 marks]

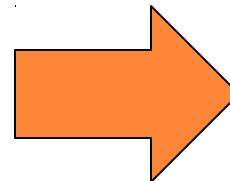
*Penyelesaian*

- - $\log_5(4x - 7) = \log_5(x - 2) + \log_5 5$
  - 
  - $\log_5(4x - 7) = \log_5(x - 2) 5$  B1
  - 
  - $(4x - 7) = (x - 2) 5$
  
  - $4x - 7 = 5x - 10$  B1
  
  - $x = 3$  B1
  -
- 



# **Contoh Soalan Kertas**

## **2**



# PERSAMAAN SERENTAK

- 1 Solve the simultaneous equations  $k - 3p = -1$  and  $p + pk - 2k = 0$ .

Give your answers correct to three decimal places.

[5 marks]

*Selesaikan persamaan serentak  $k - 3p = -1$  dan  $p + pk - 2k = 0$ .*

*Beri jawapan anda betul kepada tiga tempat perpuluhan.*

[5 markah]



$$\textcircled{1} \quad K - 3P = -1 \quad \text{--- (1)}$$

$$P + PK - 2K = 0 \quad \text{--- (2)}$$

From (1)

$$K = 3P - 1 \quad \text{--- (3)}$$

Substitute  $K = 3P - 1$  into (2)

$$P + P(3P - 1) - 2(3P - 1) = 0$$

$$P + 3P^2 - P - 6P + 2 = 0$$

$$3P^2 - 6P + 2 = 0$$

$$P = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(3)(2)}}{2(3)}$$

$$P = 1.577 \quad \text{or} \quad P = 0.423$$

Substitute  $P$  into (3)

when  $P = 1.577$

$$K = 3P - 1$$

$$= 3(1.577) - 1$$

$$= 3.731$$

N1

when  $P = 0.423$

$$K = 3P - 1$$

$$= 3(0.423) - 1$$

$$= 0.269$$

P1

OR

From (1)

$$3P = K + 1$$

$$P = \frac{K+1}{3} \quad \text{--- (3)}$$

Substitute  $P = \frac{K+1}{3}$  into (2)

$$\frac{K+1}{3} + \left(\frac{K+1}{3}\right)K - 2K = 0$$

$$K + 1 + K^2 + K - 6K = 0$$

$$K^2 - 4K + 1 = 0$$

$$K = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(1)(1)}}{2(1)}$$

$$K = 3.732 \quad \text{or} \quad K = 0.268$$

Substitute  $P$  into (3)

when  $K = 3.732$

$$P = \frac{K+1}{3}$$

$$= \frac{3.732+1}{3}$$

$$= 1.577$$

when  $K = 0.268$

$$P = \frac{0.268+1}{3}$$

$$= 0.423$$

# FUNGSI KUADRATIK

Diberi fungsi kuadratik  $f(x) = -4x^2 + 2x - 3$ .

- (a) Tulis fungsi kuadratik di atas dalam bentuk  $f(x) = a(x+p)^2 + q$ .
- (b) Cari
  - (i) titik maksimum atau titik minimum,
  - (ii) persamaan paksi simetri.
- (c) lakarkan fungsi kuadratik tersebut bagi domain  $-1 < x < 2$



## Penyelesian :

(a)  $f(x) = -4x^2 + 2x - 3 = -4(x^2 - \frac{1}{2}x) - 3$   
 $= -4 [(x-1/4)^2 - (1/4)^2] - 3 \quad \mathbf{K1}$   
 $= -4 (x-1/4)^2 - 11/4 \quad \mathbf{N1}$

(bi) titik maksimum = (  $\frac{1}{4}$  ,  $-11/4$ )  $\quad \mathbf{N1}$

(bii)  $x = \frac{1}{4} \quad \mathbf{N1}$

(c) Draw on the board



- 3 The gradient function of a curve is  $hx^2 - kx$ , where  $h$  and  $k$  are constants. The curve has a turning point at  $(3, -4)$ . The gradient of the tangent to the curve at the point  $x = -1$  is 8.

*Fungsi kecerunan suatu lengkung ialah  $hx^2 - kx$ , dengan keadaan  $h$  dan  $k$  ialah pemalar. Lengkung itu mempunyai titik pusingan pada  $(3, -4)$ . Kecerunan tangen kepada lengkung itu pada titik  $x = -1$  ialah 8.*

Find

Cari

(a) the value of  $h$  and of  $k$ , [5 marks]

*nilai  $h$  dan nilai  $k$ ,* [5 markah]

(b) the equation of the curve. [3 marks]

*persamaan lengkung itu.* [3 markah]



$$\textcircled{3} \quad \frac{dy}{dx} = hx^2 - kx$$

(a) Given  $\frac{dy}{dx} = 0$  at  $(3, -4)$

$$h(3)^2 - k(3) = 0$$

$$9h - 3k = 0$$

$$3h - k = 0 \quad \text{--- (1)}$$

K1

Given  $\frac{dy}{dx} = 8$  when  $x = -1$

$$h(-1)^2 - k(-1) = 8$$

$$h + k = 8 \quad \text{--- (2)}$$

$$3h - k = 0 \quad \text{--- (1)}$$

$$h + k = 8 \quad \text{--- (2)}$$

$$4h = 8$$

$$h = 2$$

when  $h = 2$

K1

K1

N1

$$h + k = 8$$

$$2 + k = 8$$

$$k = 6$$

N1

N1

b) Equation of the curve

$$y = \int (2x^2 - 6x) dx$$

$$= \frac{2x^3}{3} - \frac{6x^2}{2} + C$$

K1

$$y = \frac{2x^3}{3} - 3x^2 + C$$

$(3, -4)$  : sub  $x = 3, y = -4$

$$-4 = \frac{2(3)^3}{3} - 3(3)^2 + C$$

$$-4 = -9 + C$$

$$5 = C$$

$$y = \frac{2x^3}{3} - 3x^2 + 5$$

K1

N1

- 4 (a) Sketch the graph of  $y = \frac{3}{2} \cos 2x$  for  $0 \leq x \leq \frac{3}{2}\pi$ . [3 marks]

Lakar graf  $y = \frac{3}{2} \cos 2x$  untuk  $0 \leq x \leq \frac{3}{2}\pi$ . [3 markah]

- (b) Hence, using the same axes, sketch a suitable straight line to find the number of

solutions for the equation  $\frac{4}{3\pi}x - \cos 2x = \frac{3}{2}$  for  $0 \leq x \leq \frac{3}{2}\pi$ .

State the number of solutions. [3 marks]

Seterusnya, dengan menggunakan paksi yang sama, lakar satu garis lurus yang sesuai untuk mencari bilangan penyelesaian bagi persamaan

$\frac{4}{3\pi}x - \cos 2x = \frac{3}{2}$  untuk  $0 \leq x \leq \frac{3}{2}\pi$ .

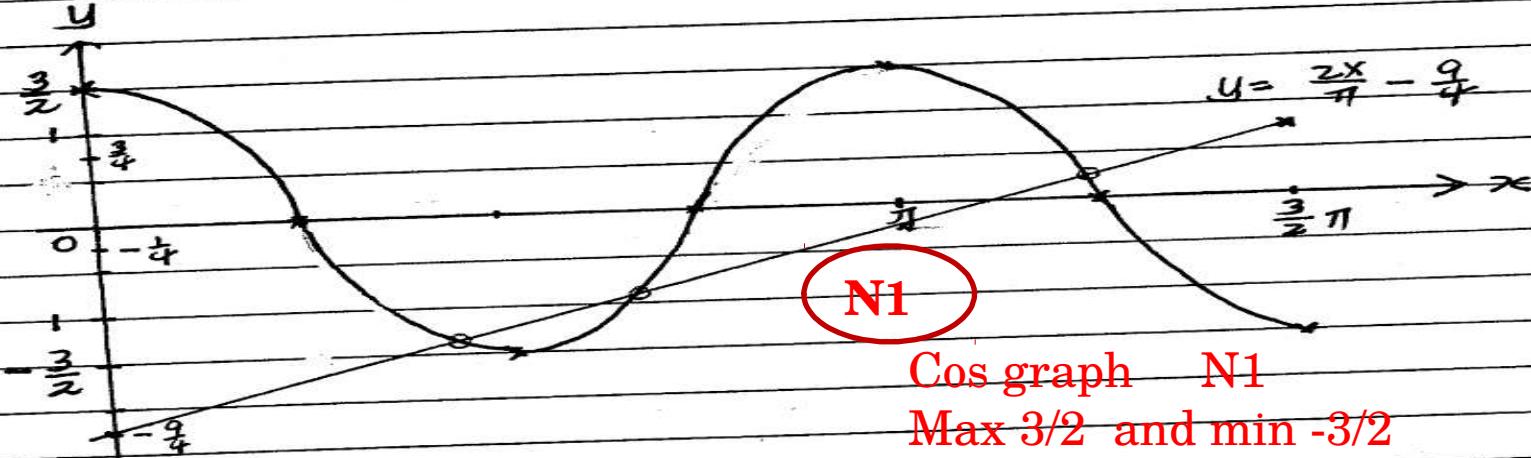
Nyatakan bilangan penyelesaian itu. [3 markah]



Perkara

(4)

(a)  $y = \frac{3}{2} \cos 2x$ ,  $0 \leq x \leq \frac{3}{2}\pi$



N1

Cos graph N1

Max  $\frac{3}{2}$  and min  $-\frac{3}{2}$   
 $\frac{3}{2}$  cycles

(b)  $\frac{4}{3}\pi - \cos 2x = \frac{3}{2}$

$$\cos 2x = \frac{4x}{3\pi} - \frac{3}{2}$$

$$\frac{3}{2} \cos 2x = \frac{3}{2} \left( \frac{4x}{3\pi} - \frac{3}{2} \right)$$

$$y = \frac{2x}{\pi} - \frac{9}{4}$$

K1

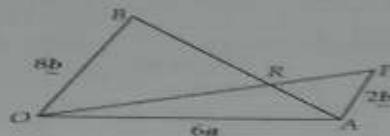
x	0	$\pi$	$\frac{3}{2}\pi$
y	$-\frac{9}{4}$	$-\frac{1}{4}$	$\frac{3}{4}$

The number of solutions = 3

N1

# VEKTOR

- 8** Diagram 8 shows two triangles  $OAB$  and  $OAP$ . The straight line  $AB$  intersects the straight line  $OP$  at  $R$ . Given  $\overrightarrow{OA} = 6\mathbf{g}$ ,  $\overrightarrow{OB} = 8\mathbf{h}$  and  $\overrightarrow{AP} = 2\mathbf{h}$ .  
 Rajah 8 menunjukkan dua buah segi tiga  $OAB$  dan  $OAP$ . Garis lurus  $AB$  bersilang dengan garis lurus  $OP$  di  $R$ . Diberi  $\overrightarrow{OA} = 6\mathbf{g}$ ,  $\overrightarrow{OB} = 8\mathbf{h}$  dan  $\overrightarrow{AP} = 2\mathbf{h}$ .



Diagram/Rajah 8

- (a) Find  
 Cari  
 (i)  $\overrightarrow{OP}$ ,  
 (ii)  $\overrightarrow{BA}$ . [2 marks]
- (b) Given that  $\overrightarrow{OR} = h\overrightarrow{OP}$  and  $\overrightarrow{BR} = k\overrightarrow{BA}$ , express  $\overrightarrow{OR}$ ,  
 Diberi bahawa  $\overrightarrow{OR} = h\overrightarrow{OP}$  dan  $\overrightarrow{BR} = k\overrightarrow{BA}$ , ungkapkan  $\overrightarrow{OR}$ ,  
 (i) in terms of  $h$ ,  $\mathbf{g}$  and  $\mathbf{h}$ ,  
 dalam sebutan  $h$ ,  $\mathbf{g}$  dan  $\mathbf{h}$ ,  
 (ii) in terms of  $k$ ,  $\mathbf{g}$  and  $\mathbf{h}$ ,  
 dalam sebutan  $k$ ,  $\mathbf{g}$  dan  $\mathbf{h}$ . [4 marks]
- (c) Using  $\overrightarrow{OR}$  from (b), find the values of  $h$  and  $k$ .  
 Dengan menggunakan  $\overrightarrow{OR}$  dari (b), cari nilai  $h$  dan  $k$ . [4 marks]

Answers:

Jawapan:

$$\begin{aligned}(a) \text{(i)} \quad \overrightarrow{OP} &= \overrightarrow{OA} + \overrightarrow{AP} \\ &= 6\mathbf{g} + 2\mathbf{h} \\ \text{(ii)} \quad \overrightarrow{BA} &= \overrightarrow{BO} + \overrightarrow{OA} \\ &= -8\mathbf{h} + 6\mathbf{g}\end{aligned}$$

$$\begin{aligned}(c) \quad 6h\mathbf{g} + 2h\mathbf{h} &= 6k\mathbf{g} + 8(1-k)\mathbf{h} \\ \therefore 6h &= 6k \quad \text{and} \quad 2h = 8(1-k) \\ h &= k \\ 2h &= 8 - 8k, \quad \text{given } h = k \\ 2k &= 8 - 8k \\ 10k &= 8\end{aligned}$$

$$\begin{aligned}k &= \frac{8}{10} = \frac{4}{5} \\ h &= \frac{4}{5}\end{aligned}$$

$$\begin{aligned}(b) \text{(i)} \quad \overrightarrow{OR} &= h\overrightarrow{OP} \\ &= h(6\mathbf{g} + 2\mathbf{h}) \\ &= 6h\mathbf{g} + 2h\mathbf{h} \\ \text{(ii)} \quad \overrightarrow{BR} &= k\overrightarrow{BA} \\ &= k(6\mathbf{g} - 8\mathbf{h}) \\ &= 6k\mathbf{g} - 8k\mathbf{h} \\ \overrightarrow{OR} &= \overrightarrow{OB} + \overrightarrow{BR} \\ &= 8\mathbf{h} + 6\mathbf{g} - 8k\mathbf{h} \\ &= 8\mathbf{h} - 8k\mathbf{h} + 6\mathbf{g} \\ &= 6k\mathbf{g} + 8(1-k)\mathbf{h}\end{aligned}$$

- 8 Use the graph paper to answer this question.

*Gunakan kertas graf untuk menjawab soalan ini.*

Table 8 shows the values of two variables,  $x$  and  $y$ , obtained from an experiment.

The variables  $x$  and  $y$  are related by the equation  $\frac{k}{y} = \frac{p}{x} + 1$ , where  $k$  and  $p$  are constants.

*Jadual 8 menunjukkan nilai-nilai bagi dua pembolehubah,  $x$  dan  $y$ , yang diperoleh daripada suatu eksperimen. Pembolehubah  $x$  dan  $y$  dihubungkan oleh persamaan*

$\frac{k}{y} = \frac{p}{x} + 1$ , dengan keadaan  $k$  dan  $p$  ialah pemalar.

$x$	1·5	2·0	3·0	4·0	5·0	6·0
$y$	2·502	0·770	0·465	0·385	0·351	0·328

Table 8  
*Jadual 8*

- (a) Based on Table 8, construct a table for the values of  $\frac{1}{x}$  and  $\frac{1}{y}$ .

[2 marks]

*Berdasarkan Jadual 8, bina satu jadual bagi nilai-nilai  $\frac{1}{x}$  dan  $\frac{1}{y}$ .*

[2 markah]

- (b) Plot  $\frac{1}{y}$  against  $\frac{1}{x}$ , using a scale of 2 cm to 0·1 unit on the  $\frac{1}{x}$ -axis and 2 cm to 0·5 unit on the  $\frac{1}{y}$ -axis.

Hence, draw the line of best fit. [3 marks]

Plot  $\frac{1}{y}$  melawan  $\frac{1}{x}$ , menggunakan skala 2 cm kepada 0·1 unit pada paksi- $\frac{1}{x}$  dan 2 cm kepada 0·5 unit pada paksi- $\frac{1}{y}$ .

Seterusnya, lukis satu garis lurus penyuaian terbaik. [3 markah]

- (c) Use the graph in 8(b) to find the value of

Guna graf di 8(b) untuk mencari nilai

- (i)  $k$ ,
- (ii)  $p$ .

[5 marks]

[5 markah]

Perkara .....

(8) (a)  $\frac{1}{y}$  against  $\frac{1}{x}$ 

$\frac{1}{x}$	0.67	0.50	0.33	0.25	0.20	0.17	
$\frac{1}{y}$	0.40	1.30	2.15	2.60	2.85	3.05	

N1
N1

(b) Refer graph.

$$(c) \frac{K}{y} = \frac{P}{x} + 1$$

$$\frac{1}{y} = \frac{P}{Kx} + \frac{1}{K}$$

$$\frac{1}{y} = \frac{P}{K} \left( \frac{1}{x} \right) + \frac{1}{K}$$

P1
----

$$(i) \frac{1}{K} = C$$

$$\frac{1}{K} = 3.90$$

$$K = 0.26$$

K1
----

N1
----

$$(ii) \frac{P}{K} = m$$

$$\frac{P}{K} = -5.21$$

K1
----

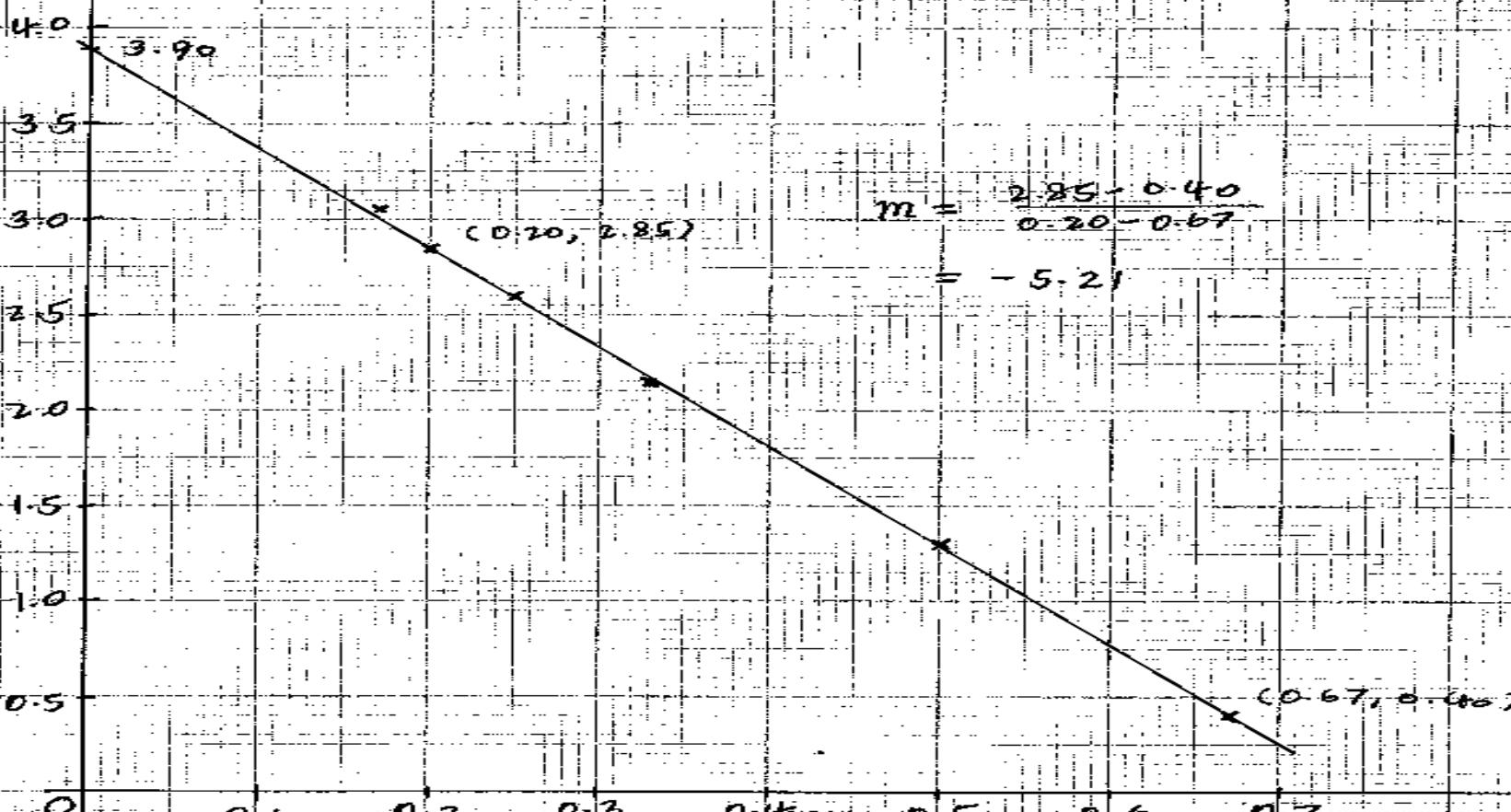
$$\frac{P}{0.26} = -5.21$$

$$P = -1.34$$

N1
----

(B) (b)

Uniform Scale :  $K_i$   
All points are plotted correctly :  $K_1$   
Line of best fit :  $N_1$



- **MODE**
- **REG**
- **LIN**
- **? , ? M+**
- **AC**
- **SHIFT 2**
- **A = PINTASAN-Y**
- **B = KECERUNAN**



9 Solution by scale drawing is not accepted.

*Penyelesaian secara lukisan berskala tidak diterima.*

Diagram 9 shows a trapezium  $OABC$ . The line  $OA$  is perpendicular to the line  $AB$ , which intersects the  $y$ -axis at the point  $Q$ . It is given that the equation of  $OA$  is

$$y = -\frac{3}{2}x \text{ and the equation of } AB \text{ is } 6y = kx + 26.$$

*Rajah 9 menunjukkan sebuah trapezium  $OABC$ . Garis  $OA$  berserenjang dengan garis  $AB$  yang bersilang dengan paksi- $y$  pada titik  $Q$ . Diberi bahawa persamaan  $OA$  ialah*

$$y = -\frac{3}{2}x \text{ dan persamaan } AB \text{ ialah } 6y = kx + 26.$$

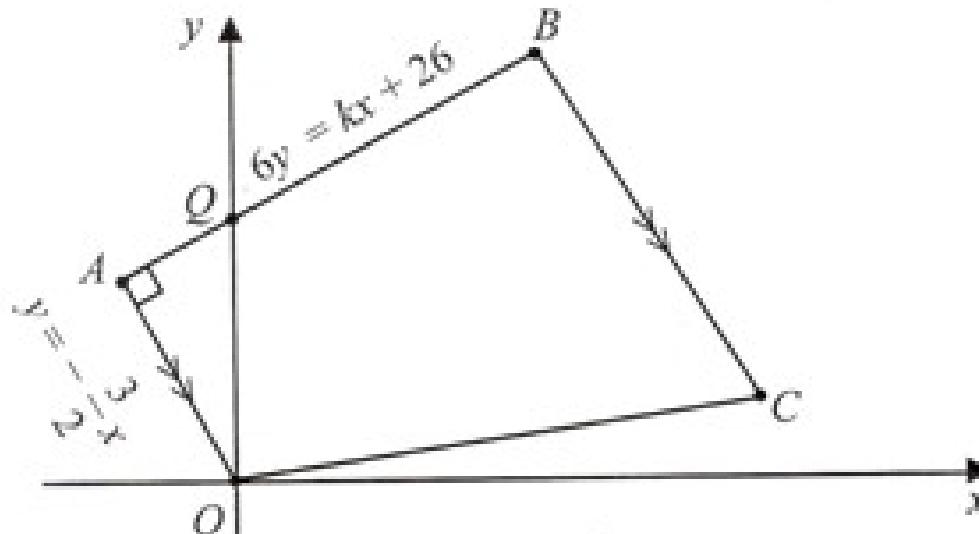


Diagram 9  
*Rajah 9*

(a) Find

Cari

- (i) the value of  $k$ ,  
*nilai  $k$ ,*
- (ii) the coordinates of  $A$ .  
*koordinat  $A$ .*

[4 marks]

[4 markah]

(b) Given  $AQ : QB = 1 : 2$ , find

Diberi  $AQ : QB = 1 : 2$ , cari

- (i) the coordinates of  $B$ ,  
*koordinat  $B$ ,*
- (ii) the equation of the straight line  $BC$ .  
*persamaan garis lurus  $BC$ .*

[4 marks]

[4 markah]

(c) A point  $P(x, y)$  moves such that  $2PA = PB$ .

Find the equation of the locus of  $P$ .

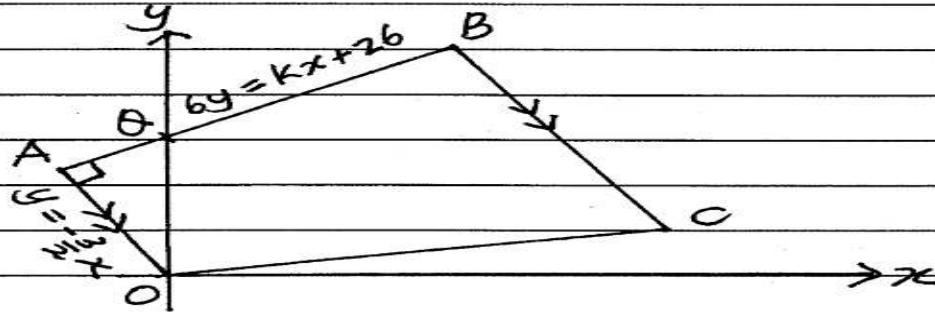
[2 marks]

Suatu titik  $P(x, y)$  bergerak dengan keadaan  $2PA = PB$ .

Cari persamaan lokus  $P$ .

[2 markah]

(a)

(a)  $(m_{OA} \times m_{AB} = -1)$  Perpendicular .

(i)

$$m_{OA} = -\frac{3}{2}$$

$$m_{AB} = \frac{k}{6}$$

$$\left(-\frac{3}{2}\right)\left(\frac{k}{6}\right) = -1$$

$$-\frac{1}{4}k = -1$$

$$k = 4$$

K1

N1

(ii) A : intersection point .

$$y = -\frac{3}{2}x \quad \text{--- (1)}$$

$$6y = 4x + 26 \quad \text{--- (2)}$$

Sub  $y = -\frac{3}{2}x$  into (2)

$$6\left(-\frac{3}{2}x\right) = 4x + 26$$

$$-9x = 4x + 26$$

$$-13x = 26$$

$$x = -2$$

K1

$$y = -\frac{3}{2}x$$

$$= -\frac{3}{2}(-2)$$

$$= 3$$

$$A(-2, 3)$$

N1

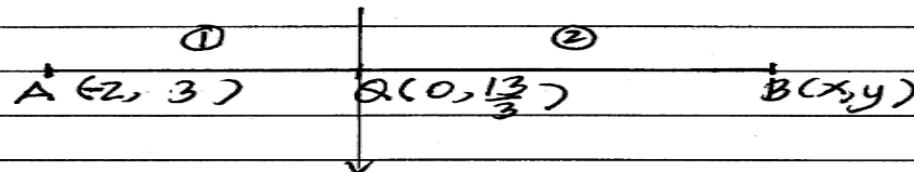
(9)

Perkara .....

(b) Q : y-intercept ( $x=0$ )

$$\text{ciri} \quad 6y = 26 \\ y = \frac{26}{6} \\ = \frac{13}{3}$$

$$Q(0, \frac{13}{3})$$



$$(0, \frac{13}{3}) = (\frac{x+2(-2)}{3}, \frac{y+2(-3)}{3})$$

K1

$$\frac{x-4}{3} = 0$$

$$x - 4 = 0$$

$$x = 4$$

$$\frac{y+6}{3} = \frac{13}{3}$$

$$y+6 = 13$$

$$y = 7$$

$$B(4, 7)$$

N1

$$\text{(ii)} \quad m_{BC} = -\frac{3}{2}, \quad B(4, 7)$$

$$y - y_1 = m(x - x_1)$$

$$y - 7 = -\frac{3}{2}(x - 4)$$

$$= -\frac{3}{2}x + 6$$

$$y = -\frac{3}{2}x + 13$$

K1

N1

$$(c) \quad 2PA = PB$$

$$2\sqrt{(x+2)^2 + (y-3)^2} = \sqrt{(x-4)^2 + (y-7)^2}$$

K1

$$4[(x+2)^2 + (y-3)^2] = (x-4)^2 + (y-7)^2$$

$$4[x^2 + 4x + 4 + y^2 - 6y + 9] = x^2 - 8x + 16 + y^2 - 14y + 49$$

$$4(x^2 + y^2 + 4x - 6y + 13) = x^2 + y^2 - 8x - 14y + 65$$

$$4x^2 + 4y^2 + 16x - 24y + 52 = x^2 + y^2 - 8x - 14y + 65$$

$$3x^2 + 3y^2 + 24x - 10y - 13 = 0$$

N1

- 10 In Diagram 10,  $POQ$  is a sector of a circle with centre  $O$  and radius 26 cm.  $SRT$  is a quadrant of a circle with centre  $R$  and radius 5 cm.

Dalam Rajah 10,  $POQ$  ialah sektor sebuah bulatan berpusat  $O$  dan berjejari 26 cm.  $SRT$  ialah sukuan sebuah bulatan berpusat  $R$  dan berjejari 5 cm.

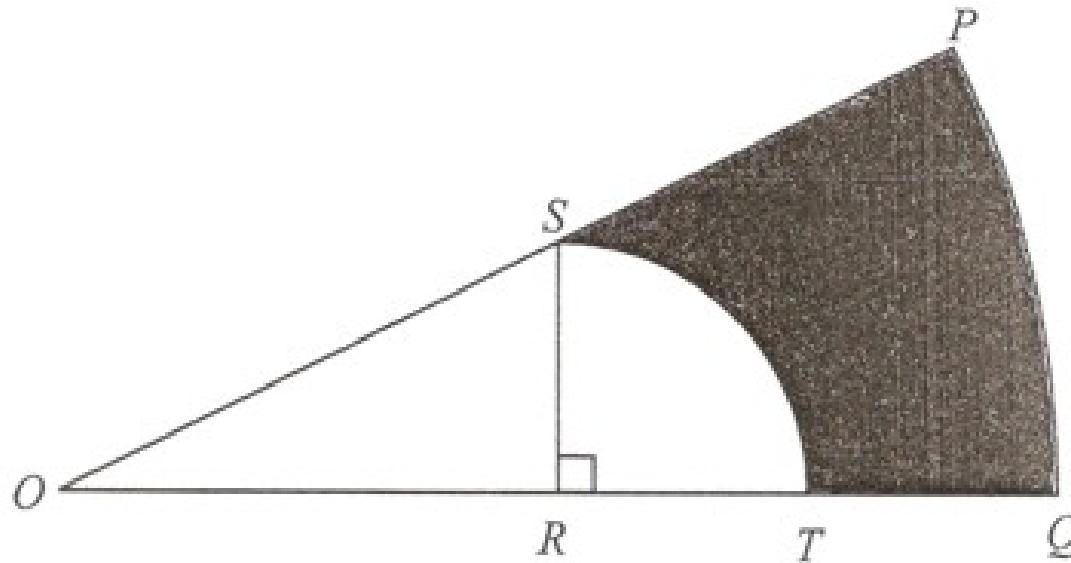


Diagram 10  
Rajah 10

It is given that  $S$  is the midpoint of  $OP$ .

Use  $\pi = 3.142$  and give the answers correct to two decimal places.

Diberi bahawa  $S$  ialah titik tengah  $OP$ .

Guna  $\pi = 3.142$  dan beri jawapan betul kepada dua tempat perpuluhan.



Calculate

*Hitung*

(a)  $\angle POQ$ , in radian, [2 marks]

*$\angle POQ$ , dalam radian,* [2 markah]

(b) the perimeter, in cm, of the coloured region, [4 marks]

*perimeter, dalam cm, kawasan berwarna,* [4 markah]

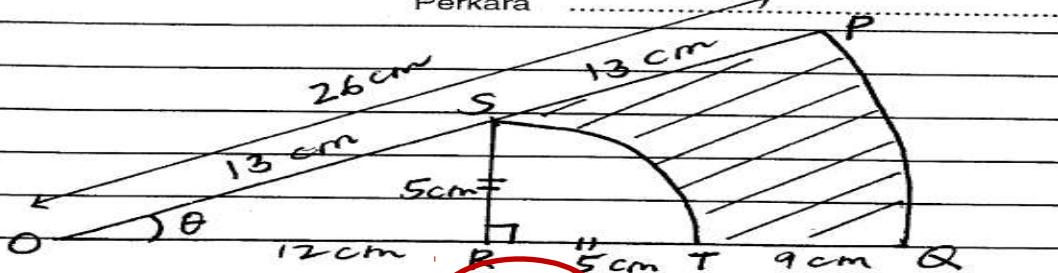
(c) the area, in  $\text{cm}^2$ , of the coloured region. [4 marks]

*luas, dalam  $\text{cm}^2$ , kawasan berwarna.* [4 markah]



(10)

Perkara .....



$$(a) \sin \theta = \frac{5}{13} \quad \text{OR} \quad \cos \theta = \frac{12}{13} \quad \text{OR} \quad \tan \theta = \frac{5}{12}$$

$$\theta = 22.62^\circ$$

$$= 22.62^\circ \times \frac{\pi}{180^\circ} = 0.3948 \text{ rad}$$

$$= 0.39 \text{ rad. (2 d.p.)}$$

N1

$$(b) \text{Perimeter} = S_{SP} + S_{PQ} + TQ$$

$$S_{SP} = r\theta$$

$$= (5) \left(\frac{\pi}{2}\right)$$

$$= 7.855$$

K1

$$S_{PQ} = r\theta$$

$$= (26) (0.39)$$

$$= 10.14$$

K1

$$TQ = 26 - 12 - 5$$

$$= 9$$

$$\text{Perimeter} = 7.855 + 10.14 + 13 + 9$$

$$= 40.00$$

N1

K1

$$(c) \text{Area of the coloured region} = A_1 - A_2 - A_3.$$

$$A_1 = \frac{1}{2} r^2 \theta$$

$$= \frac{1}{2} (26)^2 (0.39)$$

$$= 131.82$$

K1

$$A_2 = \frac{1}{2} \times 12 \times 5 \quad \text{OR} \quad A_2 = \frac{1}{2} ab \sin C$$

$$= 30$$

K1

$$= \frac{1}{2} (12)(13) \sin 22.62^\circ$$

$$= 30$$

$$A_3 = \frac{1}{2} r^2 \theta$$

$$= \frac{1}{2} (5)^2 \left(\frac{\pi}{2}\right)$$

$$= 19.64$$

$$\text{OR } A_2 = \frac{1}{2} ab \sin C$$

$$= \frac{1}{2} (13)(5) \sin 67.38^\circ$$

$$= 30$$

$$\text{Area of the coloured region} = 131.82 - 30 - 19.64$$

$$= 82.18$$

N1

K1

- 13 Table 13 shows the prices, the price indices and weightages for four types of stationery  $P$ ,  $Q$ ,  $R$  and  $S$ .

*Jadual 13 menunjukkan harga, indeks harga dan pemberat bagi empat jenis alat tulis  $P$ ,  $Q$ ,  $R$  dan  $S$ .*

Stationery <i>Alat tulis</i>	Price (RM) per unit <i>Harga (RM) per unit</i>		Price index for the year 2008 based on the year 2007 <i>Indeks harga pada tahun 2008 berasaskan tahun 2007</i>	Weightage <i>Pemberat</i>
	Year 2007 <i>Tahun 2007</i>	Year 2008 <i>Tahun 2008</i>		
$P$	2.80	2.10	$x$	4
$Q$	4.00	4.80	120	2
$R$	2.00	$y$	130	3
$S$	$z$	5.80	116	$m$

Table 13  
*Jadual 13*

(a) Find the value of

*Cari nilai*

- (i)  $x$ ,
- (ii)  $y$ ,
- (iii)  $z$ .

[3 marks]

[3 markah]

(b) The composite index for the price of the stationery in the year 2008 based on the year 2007 is 108·4.

Calculate the value of  $m$ . [3 marks]

*Indeks gubahan bagi harga alat tulis tersebut pada tahun 2008 berdasarkan tahun 2007 ialah 108·4.*

*Hitung nilai m.* [3 markah]

(c) The total expenditure for the stationery in the year 2007 is RM525.

Calculate the corresponding total expenditure in the year 2008. [2 marks]

*Jumlah perbelanjaan alat tulis tersebut pada tahun 2007 ialah RM525.*

*Hitung jumlah perbelanjaan yang sepadan pada tahun 2008.* [2 markah]

(d) The price index for  $Q$  in the year 2009 based on the year 2007 is 132.

Calculate the price index for  $Q$  in the year 2009 based on the year 2008.  
[2 marks]

*Indeks harga bagi Q pada tahun 2009 berdasarkan tahun 2007 ialah 132.*

*Hitung indeks harga bagi Q pada tahun 2009 berdasarkan tahun 2008.*  
[2 markah]



(13) (a)  $I_{0\%} = \frac{0.08}{0.07} \times 100$

(i)  $\exists x = \frac{2.10}{2.80} \times 100$   
 $= 75*$

**K1**

(ii)  $130 = \frac{y}{2.00} \times 100$   
 $y = \frac{130 \times 2.00}{100}$   
 $= 2.60*$

(iii)  $116 = \frac{5.80}{z} \times 100$

$z = \frac{5.80 \times 100}{116}$   
 $= 5*$

**B 2,1,0**

(b)  $\bar{I}_{w1} = 108.4$

$\bar{I} = \frac{\sum WI}{\sum W}$

**K1**

I	W	WI
75	4	300
120	2	240
130	3	390
116	m	116m

$\sum w = 9 + m$

$\sum WI = 930 + 116m$

**K1**

$\frac{930 + 116m}{9 + m} = 108.4$

**K1**

$930 + 116m = 108.4(9 + m)$

$= 975.6 + 108.4m$

$116m - 108.4m = 975.6 - 930$

$7.6m = 45.6$

$m = 6*$

**N1**

(13) (c)  $Q_{07} = \text{RM } 525$ 

$$Q_{08} = ?$$

$$\bar{I}_{08/07} \rightarrow \frac{Q_{08}}{Q_{07}} \times 100$$

$$108.4 = \frac{Q_{08}}{525} \times 100$$

$$Q_{08} = \frac{108.4 \times 525}{100}$$

$$= 569.10 *$$

K1

N1

$$(d) I_{09/07} = 132$$

$$I_{08/07} = 120$$

$$I_{09/08} = ?$$

$$\frac{120 \times I_{09/08}}{100} = 132$$

K1

$$I_{09/08} = \frac{132 \times 100}{120}$$

$$= 110 *$$

N1

OR

$$I_{09/07} = 132$$

$$\frac{Q_{09}}{Q_{07}} \times 100 = 132$$

$$Q_{09} = 5.28 *$$

Therefore,

$$\begin{aligned} I_{09/08} &= \frac{Q_{09}}{Q_{08}} \times 100 \\ &= \frac{5.28}{4.80} \times 100 \\ &= 110 \end{aligned}$$

$$\underline{\text{OR}} \quad I_{09/07} = 132$$

$$\frac{Q_{09}}{Q_{07}} \times 100 = 132$$

$$\frac{Q_{09}}{Q_{07}} = \frac{132}{100}$$

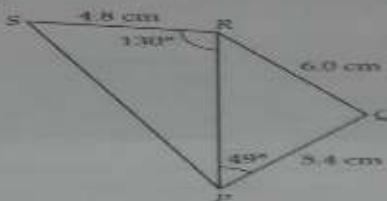
$$I_{08/07} = 120$$

$$\frac{Q_{08}}{Q_{07}} \times 100 = 120$$

$$\frac{Q_{08}}{Q_{07}} = \frac{120}{100}$$

$$\begin{aligned} \text{Therefore, } I_{09/08} &= \frac{Q_{09}}{Q_{07}} \times \frac{Q_{07}}{Q_{08}} \times 100 \\ &= \frac{132}{100} \times \frac{100}{120} \times 100 \\ &= 110 \end{aligned}$$

Diagram 14 shows a quadrilateral  $PQRS$ .  
Rajah 14 menunjukkan sebuah sisi empat  $PQRS$ .



Diagram/Rajah 14.

Calculate

*Hitung*

(a) the length, in cm, of  $PR$ ,  
*panjang, dalam cm, PR,*

[3 marks/marks]

(b) the length, in cm, of  $PS$ ,  
*panjang, dalam cm, PS,*

[3 marks/marks]

(c) the area of triangle  $PRT$ , in  $\text{cm}^2$ , if the point  $T$  lies on  $PS$  such that  $RS = RT$ .  
*luas segi tiga  $PRT$ , dalam  $\text{cm}^2$ , jika titik  $T$  terletak pada  $PS$  dengan kanduan  $RS = RT$ .* **NOTICE/CATAT**

[4 marks/marks]

Answer:

*Jawapan:*

$$(a) \frac{\sin 49^\circ}{6} = \frac{\sin R}{5.4}$$

$$\sin R = 0.6792 \\ R = 42.78^\circ$$

$$\angle Q = 180^\circ - 49^\circ - 42.78^\circ$$

$$= 88.22^\circ$$

$$\frac{PR}{\sin 88.22^\circ} = \frac{6.0}{\sin 49^\circ} \\ PR = 7.95 \text{ cm}$$

$$(b) PS^2 = PR^2 + SR^2 - 2(PR)(SR) \cos 130^\circ \\ = 7.95^2 + 4.8^2 - 2(7.95)(4.8) \cos 130^\circ \\ = 135.30 \\ PS = 11.63 \text{ cm}$$

$$(c) \frac{\sin \angle PSR}{7.95} = \frac{\sin 130^\circ}{11.63}$$

$$\sin \angle PSR = 0.5237$$

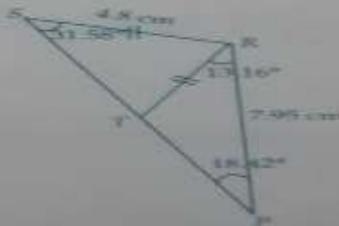
$$\angle PSR = 31.58^\circ$$

$$\angle RPS = 180^\circ - 130^\circ - 31.58^\circ$$

$$= 18.42^\circ$$

$$\angle PRT = 31.58^\circ - 18.42^\circ = 13.16^\circ$$

$$\text{Area of } \triangle PRT = \frac{1}{2} \times 4.8 \times 7.95 \times \sin 13.16^\circ \\ = 4.344 \text{ cm}^2$$

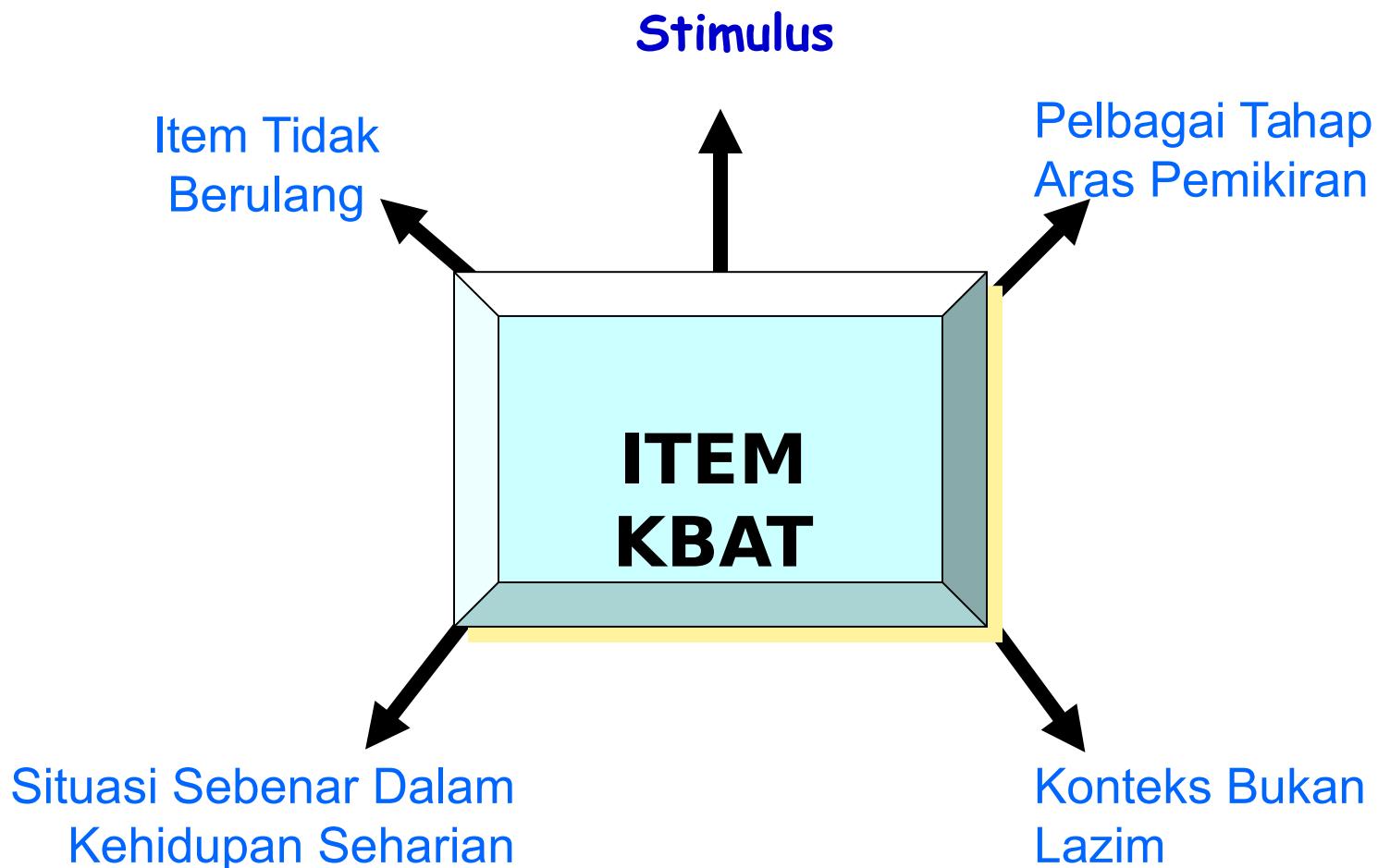


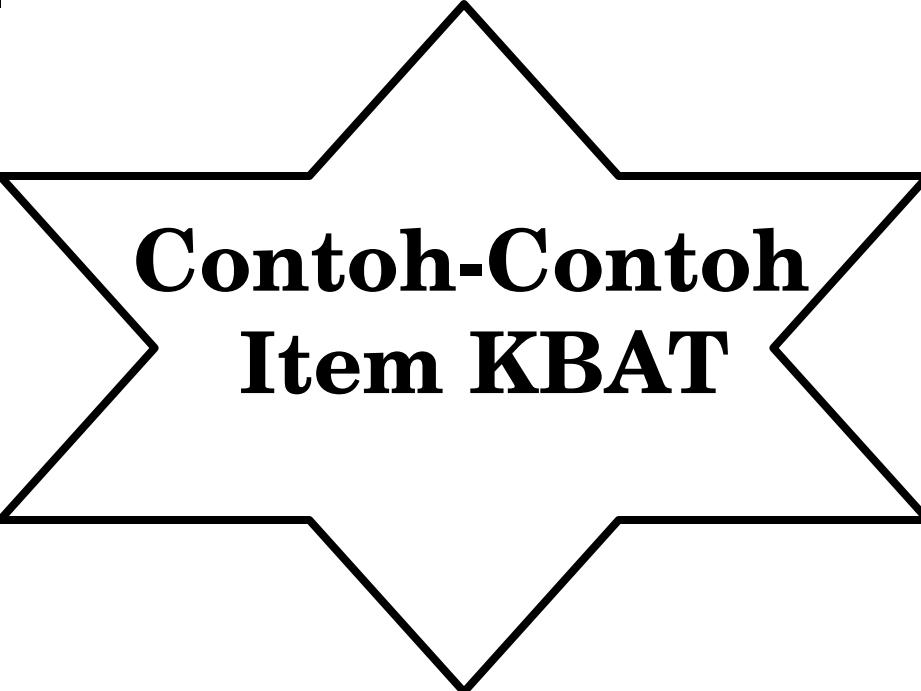
# ITEM KBAT (KEMAHIRAN BERFIKIR ARAS TINGGI)

- 2014 : 20 %
- 2015 : 30 %
- 2016 : 50 %



## **Item KBAT** **(Kemahiran Berfikir Aras Tinggi)**



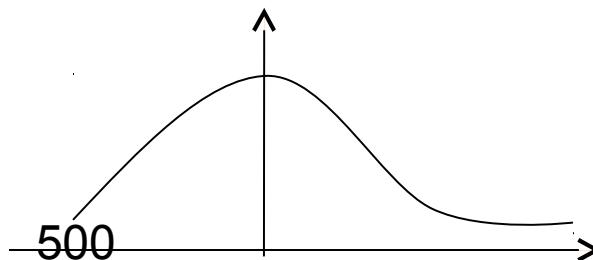


## **Contoh-Contoh Item KBAT**



# Probability Distribution

Students' intake to a certain university is determined by a certain test. The test follows a normal distribution as described by a diagram below and the standard deviation is given by 100.



Only 15 % of the students were selected to the university.

Ahmad sat for the test and obtained 590 marks. Can Ahmad enter the university?

- (a) Swee Lin sit for the test. What is the minimum mark that Swee Lin will be obtained so that she is in the highest 5 %.





**Sekian Terima Kasih**

